

WHAT IS CLAIMED IS:

1. A method for generating $(2^k - 2^t)$ first order Reed-Muller codes from 2^k first order Reed-Muller codes based on k input information bits,
5 comprising the steps of:

selecting t linearly independent k^{th} order vectors;

generating 2^t linear combinations by linearly combining the t selected vectors;

- calculating 2^t puncturing positions corresponding to the 2^t linear
10 combinations; and

generating $(2^k - 2^t)$ first order Reed-Muller codes by puncturing the 2^t puncturing positions from the 2^k first order Reed-Muller codes.

2. The method as claimed in claim 1, wherein the linearly
15 independent k^{th} order vectors satisfy a linear independent property represented by,

v^0, v^1, \dots, v^{t-1} : linear independent property

$$\Leftrightarrow c_{t-1}v^{t-1} + \dots + c_1v^1 + c_0v^0 \neq 0, \quad \forall c_0, c_1, \dots, c_{t-1}$$

3. The method as claimed in claim 1, wherein the 2^t linear
20 combinations are,

$$c^i = (c_{k-1}^i, \dots, c_1^i, c_0^i)$$

where i indicates an index for the number of the linear combinations.

4. The method as claimed in claim 1, wherein the 2^t puncturing
25 positions are calculated by converting the 2^t linear combinations to decimal numbers.

5. The method as claimed in claim 3, wherein the 2^t puncturing

positions are calculated by applying the 2^t linear combinations to an equation given below:

$$P_t = \sum_{j=0}^{k-1} c_j^t 2^j \quad t = 1, \dots, 2^t$$

5 6. The method as claimed in claim 1, wherein the 2^k first order Reed-Muller codes are codes for encoding the k input information bits.

7. The method as claimed in claim 1, wherein the 2^k first order Reed-Muller codes are a coded symbol stream obtained by encoding the k input
10 information bits with a given code.

8. A method for generating $(2^k - 2^t)$ first order Reed-Muller codes from 2^k first order Reed-Muller codes based on k input information bits, comprising the steps of:

15 selecting t linearly independent k^{th} order vectors;
 generating 2^t linear combinations by linearly combining the t selected vectors;
 calculating 2^t puncturing positions corresponding to the 2^t linear combinations;
20 selecting one $k \times k$ matrix out of a plurality of $k \times k$ matrixes having $k \times k$ inverse matrixes;
 calculating 2^t new puncturing positions by multiplying each of the 2^t puncturing positions by the selected $k \times k$ matrix; and
 generating $(2^k - 2^t)$ first order Reed-Muller codes by puncturing the 2^t new
25 puncturing positions from the 2^k first order Reed-Muller codes.

9. The method as claimed in claim 8, wherein the linearly independent k^{th} order vectors satisfy a linear independent property represented

by,

$$v^0, v^1, \dots, v^{t-1}: \text{linear independent property}$$

$$\Leftrightarrow c_{t-1}v^{t-1} + \dots + c_1v^1 + c_0v^0 \neq 0, \quad \forall c_0, c_1, \dots, c_{t-1}$$

10. The method as claimed in claim 8, wherein the 2^t linear
5 combinations are,

$$c' = (c'_{k-1}, \dots, c'_1, c'_0)$$

where i indicates an index for the number of the linear combinations.

11. The method as claimed in claim 10, wherein the 2^t puncturing
10 positions are calculated by converting the 2^t linear combinations to decimal numbers.

12. The method as claimed in claim 8, wherein the 2^t puncturing
positions are calculated by applying the 2^t linear combinations to an equation
15 given below:

$$P_t = \sum_{j=0}^{k-1} c'_j 2^j \quad t = 1, \dots, 2^t$$

13. The method as claimed in claim 8, wherein the 2^k first order
Reed-Muller codes are codes for encoding the k input information bits.
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14. The method as claimed in claim 8, wherein the 2^k first order
Reed-Muller codes are a coded symbol stream obtained by encoding the k input
information bits with a given code.

25 15. The method as claimed in claim 8, wherein the selected $k \times k$
matrix A is given as follows:

$$A = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

16. An apparatus for encoding k input information bits in a transmitter for a CDMA (Code Division Multiple Access) mobile communication system, comprising:

an encoder for encoding the k input information bits with 2^k -bit first order Reed-Muller codes, and outputting 2^k coded symbols; and

a puncturer for selecting t linearly independent k^{th} order vectors, puncturing coded symbols in puncturing positions corresponding to 2^t linear combinations, obtained by linearly combining the t selected vectors, from the 2^k coded symbols, and outputting $(2^k - 2^t)$ coded symbols.

17. The apparatus as claimed in claim 16, wherein the linearly independent k^{th} order vectors satisfy a linear independent property represented by,

$$\begin{aligned} &v^0, v^1, \dots, v^{t-1}: \text{linear independent property} \\ &\Leftrightarrow c_{t-1}v^{t-1} + \dots + c_1v^1 + c_0v^0 \neq 0, \quad \forall c_0, c_1, \dots, c_{t-1} \end{aligned}$$

18. The apparatus as claimed in claim 16, wherein the 2^t linear combinations are,

$$c^i = (c_{k-1}^i, \dots, c_1^i, c_0^i)$$

where i indicates an index for the number of the linear combinations.

19. The apparatus as claimed in claim 16, wherein the 2^t puncturing positions are calculated by converting the 2^t linear combinations to decimal numbers.

20. The apparatus as claimed in claim 18, wherein the 2^t puncturing positions are calculated by applying the 2^t linear combinations to an equation given below:

$$5 \quad P_t = \sum_{j=0}^{k-1} c_j' 2^t \quad t = 1, \dots, 2^t$$

21. An apparatus for encoding k input information bits in a transmitter for a CDMA mobile communication system, comprising:

a code generator for selecting t linearly independent k^{th} order vectors,
 10 puncturing 2^k -bit first order Reed-Muller code bits corresponding to 2^t linear combinations obtained by linearly combining the t selected vectors from the 2^k -bit first order Reed-Muller codes, and outputting $(2^k - 2^t)$ -bit first order Reed-Muller codes; and

an encoder for encoding the k input information bits with the $(2^k - 2^t)$ -bit
 15 first order Reed-Muller codes, and outputting $(2^k - 2^t)$ coded symbols.

22. The apparatus as claimed in claim 21, wherein the linearly independent k^{th} order vectors satisfy a linear independent property represented by,

$$20 \quad \begin{aligned} &v^0, v^1, \dots, v^{t-1}: \text{linear independent property} \\ &\Leftrightarrow c_{t-1}v^{t-1} + \dots + c_1v^1 + c_0v^0 \neq 0, \quad \forall c_0, c_1, \dots, c_{t-1} \end{aligned}$$

23. The apparatus as claimed in claim 21, wherein the 2^t linear combinations are,

$$c^i = (c_{k-1}', \dots, c_1', c_0')$$

25 where i indicates an index for the number of the linear combinations.

24. The apparatus as claimed in claim 21, wherein the 2^t puncturing

positions are calculated by converting the 2^t linear combinations to decimal numbers.

25. The apparatus as claimed in claim 23, wherein the 2^t puncturing
5 positions are calculated by applying the 2^t linear combinations to an equation given below:

$$P_t = \sum_{j=0}^{k-1} c_j' 2^j \quad t = 1, \dots, 2^t$$

26. The apparatus as claimed in claim 21, wherein the encoder
10 comprises:

k multipliers each for multiplying one input information bit out of the k input information bits by one $(2^k - 2^t)$ -bit first order Reed-Muller code out of the $(2^k - 2^t)$ -bit first order Reed-Muller codes, and outputting a coded symbols stream comprised of $(2^k - 2^t)$ coded symbols; and

15 a summer for summing up the coded symbol streams output from each of the k multipliers in a symbol unit, and outputting one coded symbol stream comprised of $(2^k - 2^t)$ coded symbols.

27. A method for receiving $(2^k - 2^t)$ coded symbols from a transmitter
20 and decoding k information bits from the $(2^k - 2^t)$ received coded symbols, comprising the steps of:

selecting t linearly independent k^{th} order vectors, and calculating positions corresponding to 2^t linear combinations obtained by combining the t selected vectors;

25 outputting 2^k coded symbols by inserting zero (0) bits in the calculated positions of the $(2^k - 2^t)$ coded symbols;

calculating reliabilities of respective first order Reed-Muller codes comprised of the 2^k coded symbols and 2^k bits used by the transmitter; and

decoding the k information bits from the 2^k coded symbols with a first

order Reed-Muller code having the highest reliability.

28. The method as claimed in claim 27, wherein the linearly independent k^{th} order vectors satisfy a linear independent property represented
5 by,

$$\begin{aligned} &v^0, v^1, \dots, v^{t-1}: \text{linear independent property} \\ &\Leftrightarrow c_{t-1}v^{t-1} + \dots + c_1v^1 + c_0v^0 \neq 0, \quad \forall c_0, c_1, \dots, c_{t-1} \end{aligned}$$

29. The method as claimed in claim 27, wherein the 2^t linear combinations are,

10 $c' = (c'_{k-1}, \dots, c'_1, c'_0)$

where i indicates an index for the number of the linear combinations.

30. The method as claimed in claim 27, wherein the 2^t puncturing positions are calculated by converting the 2^t linear combinations to decimal
15 numbers.

31. The method as claimed in claim 29, wherein the 2^t puncturing positions are calculated by applying the 2^t linear combinations to an equation given below:

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$$P_t = \sum_{j=0}^{k-1} c'_j 2^j \quad t = 1, \dots, 2^t$$

32. An apparatus for receiving $(2^k - 2^t)$ coded symbols from a transmitter and decoding k information bits from the $(2^k - 2^t)$ received coded symbols, comprising:

25 a zero inserter for selecting t linearly independent k^{th} order vectors, calculating positions corresponding to 2^t linear combinations obtained by combining the t selected vectors, and outputting 2^k coded symbols by inserting

an inverse fast Hadamard transform part for calculating reliabilities of respective first order Reed-Muller codes comprised of the 2^k coded symbols and 2^k bits used by the transmitter, and decoding the k information bits from the 2^k coded symbols with the first order Reed-Muller codes corresponding to the respective reliabilities; and

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